Activity Report 2014

Project-Team COMMANDS

Control, Optimization, Models, Methods and Applications for Nonlinear Dynamical Systems

IN COLLABORATION WITH: Centre de Mathématiques Appliquées (CMAP), Unité de Mathématiques Appliquées (UMA - ENSTA)
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Keywords: System Analysis And Control, Nonlinear Control, Optimal Control, Numerical Methods, Nonsmooth Analysis

Creation of the Project-Team: 2009 January 01.

1. Members

Research Scientists
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Axel Kröner [Inria, Starting Research Position, from Oct 2014]
Pierre Martinon [Inria, Researcher]
Anna Désilles [DGA]

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2. Overall Objectives

2.1. Scientific directions

Commands is a team devoted to dynamic optimization, both for deterministic and stochastic systems. This includes the following approaches: trajectory optimization, deterministic and stochastic optimal control, stochastic programming, dynamic programming and Hamilton-Jacobi-Bellman equation.

Our aim is to derive new and powerful algorithms for solving numerically these problems, with applications in several industrial fields. While the numerical aspects are the core of our approach it happens that the study of convergence of these algorithms and the verification of their well-posedness and accuracy raises interesting and difficult theoretical questions, such as, for trajectory optimization: qualification conditions and second-order optimality condition, well-posedness of the shooting algorithm, estimates for discretization errors; for the Hamilton-Jacobi-Bellman approach: accuracy estimates, strong uniqueness principles when state constraints are present, for stochastic programming problems: sensitivity analysis.
2.2. Industrial impact

For many years the team members have been deeply involved in various industrial applications, often in the framework of PhD theses or of postdocs. The Commands team itself has dealt since its foundation in 2007 with several types of applications:

- Space vehicle trajectories, in collaboration with CNES, the French space agency.
- Aeronautics, in collaboration with the startup Safety Line.
- Production, management, storage and trading of energy resources, in collaboration with EDF, GDF and TOTAL.
- Energy management for hybrid vehicles, in collaboration with Renault and IFPEN.

We give more details in the Bilateral contracts section.

3. Research Program

3.1. Historical aspects

The roots of deterministic optimal control are the “classical” theory of the calculus of variations, illustrated by the work of Newton, Bernoulli, Euler, and Lagrange (whose famous multipliers were introduced in [84]), with improvements due to the “Chicago school”, Bliss [51] during the first part of the 20th century, and by the notion of relaxed problem and generalized solution (Young [93]).

Trajectory optimization really started with the spectacular achievement done by Pontryagin’s group [90] during the fifties, by stating, for general optimal control problems, nonlocal optimality conditions generalizing those of Weierstrass. This motivated the application to many industrial problems (see the classical books by Bryson and Ho [59], Leitmann [86], Lee and Markus [85], Ioffe and Tihomirov [76]). Since then, various theoretical achievements have been obtained by extending the results to nonsmooth problems, see Aubin [47], Clarke [60], Ekeland [67].

Dynamic programming was introduced and systematically studied by R. Bellman during the fifties. The HJB equation, whose solution is the value function of the (parameterized) optimal control problem, is a variant of the classical Hamilton-Jacobi equation of mechanics for the case of dynamics parameterized by a control variable. It may be viewed as a differential form of the dynamic programming principle. This nonlinear first-order PDE appears to be well-posed in the framework of viscosity solutions introduced by Crandall and Lions [62], [63], [61]. These tools also allow to perform the numerical analysis of discretization schemes. The theoretical contributions in this direction did not cease growing, see the books by Barles [49] and Bardi and Capuzzo-Dolcetta [48].

3.2. Trajectory optimization

The so-called direct methods consist in an optimization of the trajectory, after having discretized time, by a nonlinear programming solver that possibly takes into account the dynamic structure. So the two main problems are the choice of the discretization and the nonlinear programming algorithm. A third problem is the possibility of refinement of the discretization once after solving on a coarser grid.

In the full discretization approach, general Runge-Kutta schemes with different values of control for each inner step are used. This allows to obtain and control high orders of precision, see Hager [73], Bonnans [54]. In an interior-point algorithm context, controls can be eliminated and the resulting system of equation is easily solved due to its band structure. Discretization errors due to constraints are discussed in Dontchev et al. [66]. See also Malanowski et al. [87].
In the *indirect* approach, the control is eliminated thanks to Pontryagin’s maximum principle. One has then to solve the two-points boundary value problem (with differential variables state and costate) by a single or multiple shooting method. The questions are here the choice of a discretization scheme for the integration of the boundary value problem, of a (possibly globalized) Newton type algorithm for solving the resulting finite dimensional problem in $\mathbb{R}^n$ ($n$ is the number of state variables), and a methodology for finding an initial point.

For state constrained problems or singular arcs, the formulation of the shooting function may be quite elaborate [52], [53], [46]. As initiated in [70], we focus more specifically on the handling of discontinuities, with ongoing work on the geometric integration aspects (Hamiltonian conservation).

### 3.3. Hamilton-Jacobi-Bellman approach

This approach consists in calculating the value function associated with the optimal control problem, and then synthesizing the feedback control and the optimal trajectory using Pontryagin’s principle. The method has the great particular advantage of reaching directly the global optimum, which can be very interesting when the problem is not convex.

*Characterization of the value function* >From the dynamic programming principle, we derive a characterization of the value function as being a solution (in viscosity sense) of an Hamilton-Jacobi-Bellman equation, which is a nonlinear PDE of dimension equal to the number $n$ of state variables. Since the pioneer works of Crandall and Lions [62], [63], [61], many theoretical contributions were carried out, allowing an understanding of the properties of the value function as well as of the set of admissible trajectories. However, there remains an important effort to provide for the development of effective and adapted numerical tools, mainly because of numerical complexity (complexity is exponential with respect to $n$).

*Numerical approximation for continuous value function* Several numerical schemes have been already studied to treat the case when the solution of the HJB equation (the value function) is continuous. Let us quote for example the Semi-Lagrangian methods [69], [68] studied by the team of M. Falcone (La Sapienza, Rome), the high order schemes WENO, ENO, Discrete galerkin introduced by S. Osher, C.-W. Shu, E. Harten [74], [75], [75], [88], and also the schemes on nonregular grids by R. Abgrall [45], [44]. All these schemes rely on finite differences or/and interpolation techniques which lead to numerical diffusions. Hence, the numerical solution is unsatisfying for long time approximations even in the continuous case.

One of the (nonmonotone) schemes for solving the HJB equation is based on the Ultrabee algorithm proposed, in the case of advection equation with constant velocity, by Roe [92] and recently revisited by Després-Lagoutière [65], [64]. The numerical results on several academic problems show the relevance of the antidiffusive schemes. However, the theoretical study of the convergence is a difficult question and is only partially done.

*Optimal stochastic control problems* occur when the dynamical system is uncertain. A decision typically has to be taken at each time, while realizations of future events are unknown (but some information is given on their distribution of probabilities). In particular, problems of economic nature deal with large uncertainties (on prices, production and demand). Specific examples are the portfolio selection problems in a market with risky and non-risky assets, super-replication with uncertain volatility, management of power resources (dams, gas). Air traffic control is another example of such problems.

*Nonsmoothness of the value function.* Sometimes the value function is smooth (e.g. in the case of Merton’s portfolio problem, Oksendal [94]) and the associated HJB equation can be solved explicitly. Still, the value function is not smooth enough to satisfy the HJB equation in the classical sense. As for the deterministic case, the notion of viscosity solution provides a convenient framework for dealing with the lack of smoothness, see Pham [89], that happens also to be well adapted to the study of discretization errors for numerical discretization schemes [77], [50].

*Numerical approximation for optimal stochastic control problems.* The numerical discretization of second order HJB equations was the subject of several contributions. The book of Kushner-Dupuis [83] gives a complete synthesis on the Markov chain schemes (i.e Finite Differences, semi-Lagrangian, Finite Elements,
Here a main difficulty of these equations comes from the fact that the second order operator (i.e. the diffusion term) is not uniformly elliptic and can be degenerated. Moreover, the diffusion term (covariance matrix) may change direction at any space point and at any time (this matrix is associated the dynamics volatility).

For solving stochastic control problems, we studied the so-called Generalized Finite Differences (GFD), that allow to choose at any node, the stencil approximating the diffusion matrix up to a certain threshold [57]. Determining the stencil and the associated coefficients boils down to a quadratic program to be solved at each point of the grid, and for each control. This is definitely expensive, with the exception of special structures where the coefficients can be computed at low cost. For two dimensional systems, we designed a (very) fast algorithm for computing the coefficients of the GFD scheme, based on the Stern-Brocot tree [56].

4. Application Domains

4.1. Energy production planning  
We work with colleagues from U. Chile, in the framework of Inria Chile, on the management of electricity production and storage for a microgrid.

4.2. Fuel saving by optimizing airplanes trajectories  
We have a collaboration with the startup Safety Line on the optimization of trajectories for civil aircrafts.

4.3. Hybrid vehicles  
We have a collaboration with IFPEN on the energy management for hybrid vehicles.

5. New Software and Platforms

5.1. Bocop  
Participants: Pierre Martinon [corresponding author], Frédéric Bonnans, Daphné Giorgi, Olivier Tissot.  
Web page: http://bocop.org  
The Bocop project aims to develop an open-source toolbox for solving optimal control problems, with collaborations with industrial and academic partners. Optimal control (optimization of dynamical systems governed by differential equations) has numerous applications in transportation, energy, process optimization, and biology. The software reuses some packages from the COIN-OR library, in particular the well-known nonlinear programming solver Ipopt, features a user-friendly interface and can be deployed on Windows / Mac / Linux.

The project is supported by Inria with the recruitment of Vincent Grelard as developer in 2010-2012, Daphné Giorgi (Oct. 2012-Sept. 2014), and Olivier Tissot since October 2014. The first prototype was released at the end of 2011, Bocop is currently at version 2.0.1 and has been downloaded more than 700 times. The software was first successfully tested on several academic problems, see [55] available on http://bocop.org. Starting in 2012, several research collaborations were initiated in fields such as bio-reactors for energy production ([13], [26]), swimming micro-robots ([71]), and quantum control for medical imaging ([35]). Bocop was also featured during our participation in the Imatch “Optimisation and Control” in October 2013, leading to an ongoing contract with the startup Safety Line, on fuel optimization for civil aircrafts.

Bocop auto-assessment according to Inria notice: A3up4, SO3, SM3, EM3up4, SDL4up5
6. New Results

6.1. Highlights of the Year

6.1.1. Optimization of running strategies based on anaerobic energy and variations of velocity

Participant: Frédéric Bonnans.

The paper [10] about running strategies proves Keller's conjecture. It was highlighted in SIAM Connect, see http://connect.siam.org/insightful-mathematics-for-an-optimal-run/

6.1.2. Research and transfer collaboration in aeronautics with the startup Safety Line

Participants: Frédéric Bonnans, Daphné Giorgi, Stéphan Maindrault, Pierre Martinon.

Following the meeting with the startup Safety Line at Imatch "Optimisation and Control" in october 2013, we conducted a first collaboration of six months on optimizing the fuel consumption of civil airliners. This first step successfully established the proof of concept and was validated by actual test flights in June 2014, leading to a shared patent and the development of a specific module of our software 'Bocop', included in the tool 'OptiClimb' developed at Safety Line. Future prospects include improving the numerical robustness of the current tool, as well as expanding the optimization to the cruise flight in addition to the climb phase.
6.2. Second order analysis of deterministic optimal control problems

Participant: Frédéric Bonnans.

F. Bonnans, with M.S. Aronna (IMPA, Rio de Janeiro) and B.-S. Goh (Curtin U., Miri, Sarawak, Malaysia) obtained in [32] new second order necessary and sufficient optimality conditions for a class of control-affine problems with a scalar control and a scalar state constraint. These optimality conditions extend to the constrained state framework the Goh transform, which is the classical tool for obtaining an extension of the Legendre condition. We propose a shooting algorithm to solve numerically this class of problems and we provide a sufficient condition for its local convergence. We provide examples to illustrate the theory. An article by F. Bonnans, X. Dupuis (Ceremade, U. Dauphine) and L. Pfeiffer (U. Graz) has been published in the SIAM J. Control Optim. on “Second-order necessary conditions in Pontryagin form for optimal control problems” [16].

6.3. Stochastic optimization

6.3.1. Stochastic control

Participant: Frédéric Bonnans.

With J. Gianatti (U. Rosario) and F. Silva (U. Limoges) we obtained an extension of the Sakawa-Shindo algorithm (for computing a solution of the optimality system of a deterministic optimal control problem) to stochastic control problems. The paper is in progress.

6.3.2. Stochastic programming

Participants: Frédéric Bonnans, Nicolas Grebille, Faisal Wahid.

In the framework of the thesis of Nicolas Grébille, we continued our study of decomposition algorithms for a stochastic model of optimal electricity energy production. The energy production is divided in a number of zones. The idea is to constrain the energy flows between these zones, by linear feedback to the demand (which is a random variable). The coefficients of the feedback are to be optimized. Then the problem is decomposed for each zone (and can then be solved easily by a SDDP type algorithm). We obtained encouraging preliminary numerical results in a three zones problem.

Faisal Wahid developed a mixed integer program model for hydro-power producers participating in the future intra-day French Electricity Balancing Market. He has also formulated the mixed integer stochastic dynamic program model for the more general hydro-bidding under uncertainty. The objective of this model is to produce optimal offer policies in the form of supply curves under a time inhomogeneous Markov process of electricity market clearing prices.

6.3.3. Dynamic programming and error estimates for stochastic control problems with maximum cost

Participants: Athena Picarelli, Hasnaa Zidani.

The paper [14] is concerned with stochastic optimal control for a running maximum cost. A direct approach based on dynamic programming techniques is studied leading to the characterization of the value function as the unique viscosity solution of a second order Hamilton-Jacobi-Bellman (HJB) equation with an oblique derivative boundary condition. A general numerical scheme is proposed and a convergence result is provided. Error estimates are obtained for the semi-Lagrangian scheme. These results can apply to the case of lookback options in finance. Moreover, optimal control problems with maximum cost arise in the characterization of the reachable sets for a system of controlled stochastic differential equations. Some numerical simulations on examples of reachable analysis are included to illustrate our approach.

6.4. Hamilton Jacobi Bellman approach

6.4.1. Optimal feedback control of undamped wave equations by solving a HJB equation

Participants: Hasnaa Zidani, Axel Kröner.
An optimal finite-time horizon feedback control problem for (semi linear) wave equations is studied in [25]. The feedback law can be derived from the dynamic programming principle and requires to solve the evolutionary Hamilton-Jacobi-Bellman (HJB) equation. Classical discretization methods based on finite elements lead to approximated problems governed by ODEs in high dimensional space which makes infeasible the numerical resolution by HJB approach. In the present paper, an approximation based on spectral elements is used to discretize the wave equation. The effect of noise is considered and numerical simulations are presented to show the relevance of the approach.

6.4.2. Transmission conditions on interfaces for Hamilton-Jacobi-Bellman equations

Participant: Hasnaa Zidani.

The works [27], [91] deal with deterministic control problems where the dynamic and the running cost can be completely different in two (or more) complementary domains of the space $\mathbb{R}^N$. As a consequence, the dynamics and running cost present discontinuities at the interfaces of these domains. This leads to a complex interplay that has to be analyzed among transmission conditions to "glue" the propagation of the value function on the interfaces. Several questions arise: how to define properly the value function(s) and what is (are) the right Bellman Equation(s) associated with this problem?. In the case of a simple geometry (namely when the space $\mathbb{R}^N$ is partitioned into two subdomains separated with an interface which is assumed to be a regular hypersurface without any connectedness requirement), [27] discuss different conditions on the hyperplane where the dynamic and the running cost are discontinuous, and the uniqueness properties of the Bellman problem are studied. In this paper we use a dynamical approach, namely instead of working with test functions, the accent is put on invariance properties of an augmented dynamics related to the integrated control system. The comparison principle is accordingly based, rather than on (semi)continuity of the Hamiltonian appearing in the Hamilton–Jacobi–Bellman equation, on some weak separation properties of this dynamics with respect to the stratification.

6.4.3. Control Problems on Stratifiable state-constraints Sets

Participants: Cristopher Hermosilla, Hasnaa Zidani.

This work deals with a state-constrained control problem. It is well known that, unless some compatibility condition between constraints and dynamics holds, the value function has not enough regularity, or can fail to be the unique constrained viscosity solution of a Hamilton-Jacobi-Bellman (HJB) equation. Here, we consider the case of a set of constraints having a stratified structure. Under this circumstance, the interior of this set may be empty or disconnected, and the admissible trajectories may have the only option to stay on the boundary without possible approximation in the interior of the constraints. In such situations, the classical pointing qualification hypothesis are not relevant. The discontinuous Value Function is then characterized by means of a system of HJB equations on each stratum that composes the state-constraints. This result is obtained under a local controllability assumption which is required only on the strata where some chattering phenomena could occur.

6.4.4. Constrained optimization problems in finite and infinite dimensional spaces

Participant: Cristopher Hermosilla.

We investigate in [39] convex constrained nonlinear optimization problems and optimal control with convex state constraints. For this purpose we endow the interior of constraints set with the structure of Riemannian manifold. In particular, we consider a class of Riemannian metric induced by the squared Hessian of a Legendre functions. We describe in details the geodesic curves on this manifolds and we propose a gradient-like algorithm for constrained optimization based on linear search along geodesics. We also use the Legendre change of coordinates to study the Value Function of a Mayer problem with state constraints. We provide a characterization of the Value Function for this problem as the unique viscosity solution of the Hamilton-Jacobi-Bellman equation.
6.5. Robustness of discontinuous Feedbacks

Participant: Cristopher Hermosilla.

In the paper [40] we study state-constrained discontinuous ordinary differential equations for which the corresponding vector field has a set of singularities that forms a stratification of the state domain. Existence of solutions and robustness with respect to external perturbations of the righthand term are investigated. Moreover, notions of regularity for stratifications are discussed.

6.6. Optimal control of PDEs

6.6.1. Closed-loop optimal control of PDEs

Participant: Axel Kröner.

Stabilization of Burgers equation to nonstationary trajectories A. Kröner and Sérgio S. Rodrigues (RICAM, Linz, Austria) considered in [82] using infinite-dimensional internal controls. Estimates for the dimension of the controller are derived; in the particular case of no constraint in the support of the control a better estimate is derived and the possibility of getting an analogous estimate for the general case is discussed. Numerical examples are presented illustrating the stabilizing effect of the feedback control, and suggesting that the existence of an estimate in the general case analogous to that in the particular one is plausible. In [81] the problem was considered for a finite number of internal piecewise constant controls.

Reduced-order minimum time control of advection-reaction -diffusion systems via dynamic programming Dante Kalise (RICAM, Linz, Austria) and A. Kröner considered in [79]. The authors use balanced truncation for the model reduction part and include a Luenberger observer.

A semi-Lagrangian scheme for \( L^p \)-penalized minimum time problems was considered by M. Falcone (Sapienza-Università di Roma, Italy), D. Kalise (RICAM, Austria) and A. Kröner in [78].

6.6.2. Open-loop optimal control of PDEs

Participant: Axel Kröner.

The minimum effort problem for the wave equation K. Kunisch (University of Graz, Austria) and A. Kröner considered in [80]. The problem involves \( L^\infty \)-control costs which lead to non-differentiability. Uniqueness of the solution of a regularized problem is proven and the convergence of the regularized solutions is analyzed. Further, a semi-smooth Newton method is formulated to solve the regularized problems and its superlinear convergence is shown. Numerical examples confirm the theoretical results.

6.7. Applications in deterministic optimal control

6.7.1. Contrast imaging problem in nuclear magnetic resonance

Participant: Pierre Martinon.

In collaboration with team McTAO (Sophia), we started in 2013 to study the contrast imaging problem in nuclear magnetic resonance, modeled as Mayer problem in optimal control ( [58]). Using tools from the Maximum Principle and geometric control, we obtained a first synthesis of locally optimal solutions is given in the single-input case, as well as preliminary results in the bi-input case. This analysis was supported by comprehensive numerical investigations using a combination of indirect shooting (HAMPATH software) and direct method (BOCOP), with a moment-based (LMI) technique to estimate the global optimum. These results have been extended in 2014, on the theoretical side with the classification of singular extremals ([35]), and on the numerical side with the study of a large number of spins particles subject to spatial inhomogeneities in the magnetic field.

6.7.2. Optimal strokes and design for N-link microswimmer

Participant: Pierre Martinon.
Following [71], we pursued the study of the N-link swimmer, a generalization of the classical Purcell swimmer. We use the model of the Resistive Force Theory to derive the motion equation for the swimmer in a fluid with a low Reynolds number. This allows us to study and solve the optimal swimming problem in the framework of optimal control. We extend our previous study of the optimal strokes by moving to the optimal design of the swimmer. In [72] we provide an estimate of the optimal link ratio for maximal displacement, based on an expansion for small amplitudes. This theoretical result is supported by numerical simulations, that also give some insight on the type of optimal strokes depending on the constraints on the amplitude and deformation speed.

6.7.3. Energy management for a micro-grid

Participants: Frédéric Bonnans, Daphné Giorgi, Benjamin Heymann, Stéphan Maindrault, Pierre Martinon.

We study the energy management problem for a microgrid including a diesel generator and a photovoltaic plant with a battery storage system. The objective is to minimize the total operational cost over a certain timeframe, primarily the diesel consumption, while satisfying a prescribed power load. After reformulation, the decision variables can be reduced to the charging/discharging power for the battery system. We take into account the switching cost for the diesel generator, the non-convex objective, and the long-term aging of the batteries. We solve this problem using a continuous optimal control framework, with both a direct transcription method (time discretization) and a Dynamic Programming method (Hamilton Jacobi Bellman). This project is a collaboration between team COMMANDS (Inria Saclay, France) and Centro de Energia (Universidad de Chile, Chile). A first paper is currently in preparation, while ongoing studies include comparison with
the existing MILP approach, more refined battery aging models, and modeling the stochastic nature of the photovoltaic power and power load.

Figure 5. Microgrid management - Winter day sample case

7. Bilateral Contracts and Grants with Industry

7.1. Bilateral Contracts with Industry

- IFPEN, PhD thesis of F.Bleuse, ‘Optimal control and robustness for rechargeable hybrid vehicles’. The study is focused on the so-called parallel architecture, with both the thermal and electric engines able to move the vehicle. The main axis is to optimize the use of the thermal engine.
- Safety Line (startup in aeronautics), research and transfer contract, optimization of fuel consumption for civil planes. A first part is devoted to the identification of the aerodynamic and thrust characteristics of the plane, using recorded flight data. A second part is optimizing the fuel consumption during the climb phase.

8. Partnerships and Cooperations

8.1. Regional Initiatives

- F. Bonnans is coordinator of the ICODE project “Strategic crowds: analysis and simulation”, with U. Limoges, Paris-Sud.
- F. Bonnans participates to two PGMO project: “Hydro-electric scheduling under uncertainty”, with U. Auckland, “Perturbation analysis for deterministic and stochastic optimal control problems”, with U. Limoges and TSE (Toulouse),
- P. Martinon participates to the OPTIBIO project, supported by FMJH-PGMO, devoted to “New challenges in the optimal control of bioprocesses”, with U. Angers, Lille 1 / Limoges

8.2. National Initiatives

8.2.1. DGA

Participants: Olivier Bokanowski, Anna Désilles, Hasnaa Zidani.
This project is a collaboration in the framework of a 3-year (2012-2015) research program funded by DGA. The title of the project is “Problèmes de commande optimale pour des systèmes non-linéaires en présence d’incertitudes et sous contraintes de probabilité de succès”.

8.2.2. ANR HJNet
Participants: Olivier Bokanowski, Zhiping Rao, Hasnaa Zidani.

The team is part of the collaborative project HJNet funded by the French National Research Agency (ANR-12-BS01-0008-01). It started in January 2013 and will end in December 2013. Website: http://hjnet.math.cnrs.fr

8.3. European Initiatives

8.3.1. FP7 & H2020 Projects

8.3.1.1. SADCO
Type: FP7
Defi: NC
Instrument: Initial Training Network
Objectif: NC
Duration: January 2011 - December 2014
Coordinator: Inria
Inria contact: Hasnaa Zidani
Abstract: Optimisation-based control systems concern the determination of control strategies for complex, dynamic systems, to optimise some measures of best performance. It has the potential for application to a wide range of fields, including aerospace, chemical processing, power systems control, transportation systems and resource economics. It is of special relevance today, because optimization provides a natural framework for determining control strategies, which are energy efficient and respect environmental constraints. The multi-partner initial training network SADCO aims at: Training young researchers and future scientific leaders in the field of control theory with emphasis on two major themes sensitivity of optimal strategies to changes in the optimal control problem specification, and deterministic controller design; Advancing the theory and developing new numerical methods; Conveying fundamental scientific contributions within European industrial sectors.
See: http://itn-sadco.inria.fr

8.4. International Initiatives

8.4.1. Inria International Labs
We are involved in the CIRIC team “Optimization and control of energy”, jointly with U. de Chile at Santiago. This collaboration involved several visits of the team in Santiago: F. Bonnans (1 week), B. Heymann (2 months) and P. Martinon (2 weeks).

8.4.2. Inria Associate Teams

8.4.2.1. OCONET
Title: Optimization and control in network economics
International Partner:
   Universidad de Chile (CHILI)
Duration: 2012 - 2014.
Limited resources in telecommunication, energy, gas and water supply networks, lead to multi-agent interactions that can be seen as games or economic equilibrium involving stochastic optimization and optimal control problems. Interaction occurs within a network, where decisions on what to produce, consume, trade or plan, are subject to constraints imposed by node and link capacities, risk, and uncertainty, e.g. the capacity of generators and transmission lines; capacity of pipeline in gas supply; switches and antennas in telecommunication. At the same time, nonlinear phenomena arise from price formation as a consequence of demand-supply equilibria or multi-unit auction processes in the case of energy and telecommunication. We will focus first in this project in electricity markets in which there are producers/consumers PCs, and an agent called ISO (Independent system operator) in charge of the management of the network. One major application we have in mind is the one of smart (electrical) grids, in view of the increased use of renewable energies, that is, a massive entry of wind, geothermal, solar in particular.

8.4.3. Inria International Partners

8.4.3.1. Informal International Partners

Collaboration with the CIFASIS lab of U. Rosario, Argentina (3 months visit of J. Gianatti).

8.5. International Research Visitors

8.5.1. Visits of International Scientists


8.5.1.1. Internships


9. Dissemination

9.1. Promoting Scientific Activities

9.1.1. Scientific events organisation


9.1.1.1. general chair, scientific chair


9.1.1.2. member of the organizing committee


9.1.2. Scientific events selection

9.1.2.1. member of the conference program committee


9.1.3. Journal

9.1.3.1. Participation to editorial boards
- F. Bonnans is Corresponding Editor of “ESAIM:COCV” (Control, Optimization and Calculus of Variations), and Associate Editor of “Applied Mathematics and Optimization”, “Optimization, Methods and Software”, and “Series on Mathematics and its Applications, Annals of The Academy of Romanian Scientists”.
- H. Zidani is Associate Editor of “Set-Valued and Variational Analysis”, and "Communication of Pure and Applied Analysis”.

9.2. Teaching - Supervision - Juries

9.2.1. Teaching

Master
F. Bonnans: Optimal control, 10h, M2, Ensta, France.
H. Zidani: Optimal control, 10h, M2, Ensta, France.

E-learning
F. Bonnans, several lecture notes on the page http://www.cmap.polytechnique.fr/~bonnans/notes.html

9.2.2. Supervision

- PhD in progress: Benjamin Heymann, Dynamic optimization with uncertainty; application to energy production. Started October 2013, F. Bonnans, Polytechnique fellowship.
- PhD in progress: Mohamed Assellaou, Reachability analysis for stochastic controlled systems. Started October 2011, O. Bokanowski and H. Zidani.

9.3. Popularization

The paper [10] about running strategies was reported in several media in 2014, especially by Figaro (May 29), Usine Nouvelle (May 18), Science Daily (May 15), MedicalXPress (May 15), Ipodiatry (May 21) and French Huffington Post in 2013.

10. Bibliography

Major publications by the team in recent years

References


Publications of the year

Articles in International Peer-Reviewed Journals


[19] X. Dupuis. Optimal control of leukemic cell population dynamics, in "Mathematical Modeling for Natural Phenomena", 2014, vol. 9, n° 1, pp. 4-26 [DOI : 10.1051/mmnp/20149102], https://hal.inria.fr/hal-00858208


Invited Conferences


International Conferences with Proceedings


Research Reports


Patents and standards


Other Publications


[33] M. S. Aronna, M. Motta, F. Rampazzo. Quick reachability and proper extension for problems with unbounded controls, 2014, NETCO 2014, Parallel session, https://hal.inria.fr/hal-01024111

[34] J. F. Bonnans. Optimization of running strategies based on anaerobic energy and variations of velocity, June 2014, NETCO 2014, Parallel session, https://hal.inria.fr/hal-01024231


[36] P. Cardaliaguet, P. J. Graber. Mean field games systems of first order, January 2014, https://hal.archives-ouvertes.fr/hal-00925905

[38] L. GIRALDI, P. MARTINON, M. ZOPPELLO. *Optimal Design for Purcell Three-link Swimmer*, September 2014, https://hal.archives-ouvertes.fr/hal-01098501

[39] C. HERMOSILLA. *Squared hessian Riemannian metrics on convex sets and applications to finite and infinite optimization*, July 2014, https://hal.inria.fr/hal-01055917

[40] C. HERMOSILLA. *Stratified discontinuous differential equations and sufficient conditions for robustness*, January 2014, https://hal.inria.fr/hal-00955927


[42] A. KRÖNER, S. S. RODRIGUES. *Internal exponential stabilization to a nonstationary solution for 1D Burgers equations with piecewise constant controls*, December 2014, https://hal.archives-ouvertes.fr/hal-01089896

[43] A. KRÖNER, S. S. RODRIGUES. *Remarks on the internal exponential stabilization to a nonstationary solution for 1D Burgers equations*, December 2014, https://hal.archives-ouvertes.fr/hal-01089893

**References in notes**


[58] B. Bonnard, M. Claeyss, O. Cots, P. Martinon. Geometric and numerical methods in the contrast imaging problem in nuclear magnetic resonance, 2013, https://hal.inria.fr/hal-00867753


